

Modeling of enzymatic synthesis of fructooligosaccharides in continuous membrane reactors

Z. Kovács¹, L. Engel¹, K. Grau¹, T. Hahn¹,
M. Ebrahimi¹, P. Czermak^{1,2}

¹Institute of Biopharmaceutical Technology
University of Applied Sciences Giessen, Germany

²Department of Chemical Engineering
Kansas State University, Manhattan, Kansas, USA

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Outline

- 1 Introduction
- 2 Reaction kinetics
 - Network of the reaction mechanism
 - Enzyme screening
 - The reaction model
- 3 Membrane-assisted Continuous Reactor
 - Experimental
 - Process design equations
 - Operation strategies
- 4 Summary

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Introduction

Motive of the study:

- Economic significance: 33 billion USD estimated world market for functional foods
- Non-nutritive sweeteners providing 30-50% of the sweetness of table sugar
- Non-digestible dietary fibers
- Encouragement of the growth of beneficial bacteria in the colon
- Health benefits: anticancerous effects, reduction of serum cholesterol level, synthesis of B-complex vitamins, enhance absorption of dietary calcium.
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- Experimental investigation on batch and continuous FOS production
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Network of the reaction mechanism

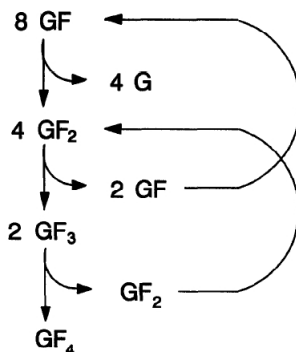


Figure: Production of fructooligosaccharides from sucrose catalyzed by fructosyltransferase derived from *Asp. pulluans*.

Enzyme screening

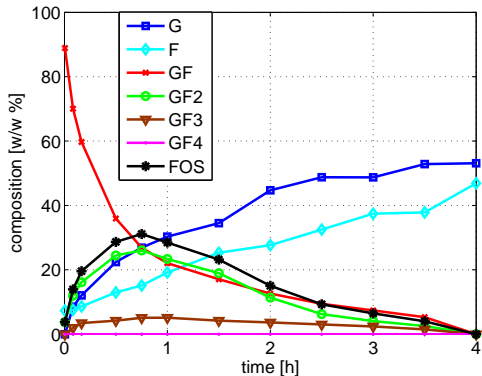
FTase activity* of commercial enzyme preparations used in fruit juice processing

Enzyme Preparation	Enzyme activity (units/ml)	Specific activity (units/mg protein)
Pectinex Ultra SP-L(Novo)	44.8	2.71
Pectinex 3XL(Novo)	9.1	0.98
Novozym 188(Novo)	32.9	0.62
Celluclast 1.5L(Novo)	0	0
Rohapect D5L Special(Rohm)	15.7	1.48
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Rohapect VRSL(Rohm)	6.9	0.67
Rohapect MA plus(Rohm)	0.39	0.12
Rohapect B1L(Rohm)	10.7	1.14
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Rapidase Liqplus(Gist-Brocades)	20.6	0.79
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Klerzyme 200(Gist-Brocades)	19.6	1.96
Cytolase CL(Gist-Brocades)	0	0
Cytolase M102(Gist-Brocades)	3.5	0.13
Cytolase PCL5(Gist-Brocades)	6.3	0.49
Cytolase 2AL(Gist-Brocades)	1.74	0.04
Clarex 5XL(Solvay)	10.6	0.94
Clarex ML(Solvay)	4.88	0.39
Pectinase AT(Solvay)	12.2	0.87

*1U is defined as the amount of FTase that transferred 1 umole of fructose per min under assay conditions (0.6M GF, pH 5.6, 40°C, 15 h).

Enzyme screening

Fructozyme L™

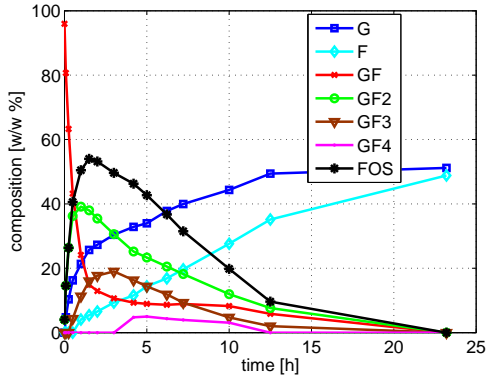


Product Characteristics:

Inulinase (EC 3.2.1.7)
from *Aspergillus niger*
Producer: Novozyme Corp.
Supplier: Sigma-Aldrich Inc.

Enzyme screening

ULTRA-Fruit™

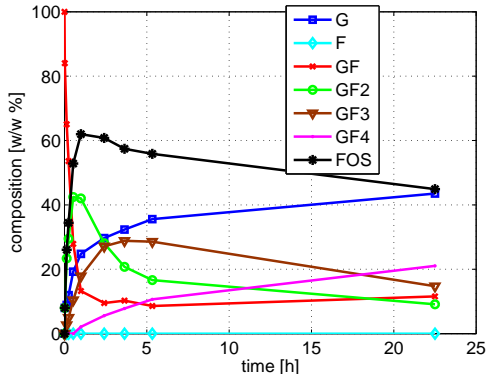


Product Characteristics:

Pectinase
from *A. niger*
and *Tr. Longibrachiatum*
Supplier: ReKru GmbH
FAO/WHO food-grade purity

Enzyme screening

Pectinex Ultra SP-L™



Product Characteristics:

Polygalacturonase
form submerged fermentation
of *Aspergillus aculeatus*
FAO/WHO food-grade purity
Physical form: Liquid
Density (g/ml): 1.16
Stabilisers: Glycerol, KCl
Preservatives: None
Colour: Brown
Producer: Novozyme Corp.
Supplier: ReKru GmbH

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The reaction model:



The Cauchy problem:

$$\begin{aligned}
 \frac{d[G]}{dt} &= r_1 + r_4 + r_5 \\
 \frac{d[GF]}{dt} &= -2r_1 + r_2 - r_4 - r_5 + r_6 \\
 \frac{d[GF_2]}{dt} &= r_1 - 2r_2 + r_3 - r_4 - r_6 \\
 \frac{d[GF_3]}{dt} &= r_2 - 2r_3 + r_4 - r_5 - r_6 \\
 \frac{d[GF_4]}{dt} &= r_3 + r_5 + r_6
 \end{aligned}$$

[Nishizawa et al. Food Sci. Technol. Res. 7 (2001) 39-44]

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Assuming a two-substrate random bi-bi model (Price & Stevens, 1989), rate equations are obtained as follows:

$$r_1 = \frac{V_{m,GF}[GF]^2}{K_{m1,GF}K_{m2,GF} + K_{m2,GF}[GF] + [GF]^2 + K_{m2,GF}[GF][G]/K_{i,n} + K_{m1,GF}K_{m2,GF}[G]/K_{i,n}}$$

$$r_2 = \frac{V_{m,GF2}[GF_2]^2}{K_{m1,GF2}K_{m2,GF2} + K_{m2,GF2}[GF_2] + [GF_2]^2}$$

$$r_3 = \frac{V_{m,GF3}[GF_3]^2}{K_{m1,GF3}K_{m2,GF3} + K_{m2,GF3}[GF_3] + [GF_3]^2}$$

$$r_4 = \frac{V_{m4}[GF][GF_2]}{K_{m1,GF}K_{m2,GF-GF2} + K_{m2,GF-GF2}[GF] + K_{m2,GF2-GF}[GF_2] + [GF][GF_2]}$$

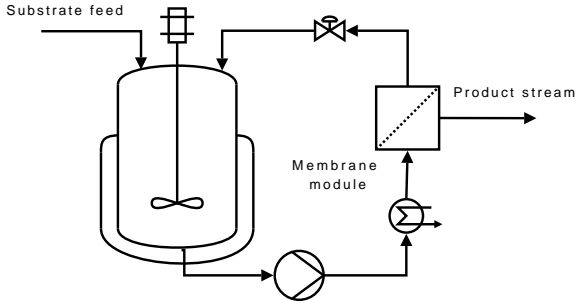
$$r_5 = \frac{V_{m5}[GF][GF_3]}{K_{m1,GF}K_{m2,GF-GF3} + K_{m2,GF-GF3}[GF] + K_{m2,GF3-GF}[GF_3] + [GF][GF_3]}$$

$$r_6 = \frac{V_{m6}[GF_2][GF_3]}{K_{m1,GF2}K_{m2,GF2-GF3} + K_{m2,GF2-GF3}[GF_2] + K_{m2,GF3-GF2}[GF_3] + [GF_2][GF_3]}$$

where V_m is the maximum transfructosylation rate, K_{m1} and K_{m2} are dissociation constants.

[Nishizawa et al. Food Sci. Technol. Res. 7 (2001) 39-44]

Membrane-assisted Continuous Stirred Tank Reactor



Manufacturer	Membrane	MWCO	Membrane material	pH range	Max. temp.
atech	UF-TiO ₂	20 kD	Al ₂ O ₃ /TiO ₂	0-14	121

Coupling MBR process design equations with enzyme kinetics model

General Mole Balance for a Continuous Chemical Reactor:

$$\frac{d}{dt} \int_V c_j dV = q_{in} c_{j,in} - q_{out} c_{j,out} + \int_V R_j dV$$

If the reactor volume is constant, the inlet and outlet flows are equal, the reactor is well stirred:

$$\frac{dc_j}{dt} = \frac{q}{V} (c_{j,in} - c_{j,out}) + R_j,$$

where $\tau=V/q$ is the residence time.

The membrane filtration is dictated by the biochemistry and not vice versa.

$$q = q(A, \mu, T, c_{prot}, \Delta P)$$

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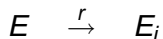
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The active enzyme E undergoes an irreversible transformation to inactive form E_i :



The rate of deactivation is a first order reaction:

$$-\frac{dc_E}{dt} = r_d = k_d c_E$$

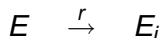
Integration gives the active enzyme concentration as a function of time:

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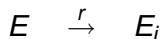
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Resting stability

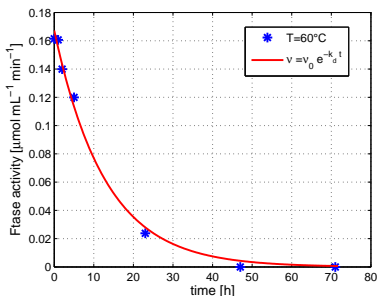


Table: Temperature dependence of deactivation rate constant and catalyst half-life

T [$^\circ\text{C}$]	pH	k_d [h^{-1}]	t_h [h]
30	6.0	0.111	6.2
40	6.0	0.004	156.2
50	6.0	0.003	223.8
60	6.0	0.078	8.9
60	4.5	0.122	5.7

Assay conditions: 500g/L GF, 100 mL/L enzyme preparation, 60 $^\circ\text{C}$, pH 5.8, KH_2PO_4 -NaOH buffer

MBR operation strategies for compensating catalysts deactivation

- Addition of fresh enzyme into the reactor to raise the concentration of active enzyme
 - requires an increase in the transmembrane pressure
- Increasing the residence time τ by decreasing the permeate flow-rate q
 - obtained by decreasing the transmembrane pressure
 - an increase of the working volume in the reactor
- Mixed-policy

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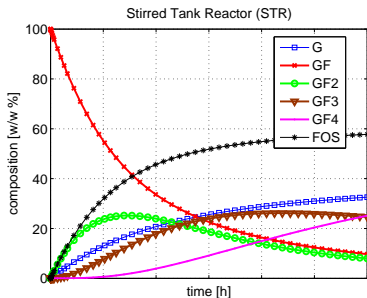
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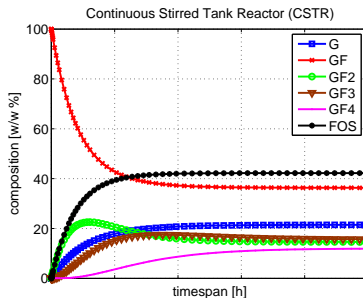
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Typical operational profiles

Dynamic evaluation of a batch FOS synthesis:



Steady-state operation performance of a continuous FOS production:



Summary

- **Mathematical model for production of FOS by a membrane-assisted CSTR is provided.**
- Mathematical framework is built by coupling the design equations of the membrane reactor configuration with the equations describing the enzyme kinetics.
- Pectinex Ultra SP-L can be utilized in an CSTR to produce high-content FOS syrup.
- Recommended for applications where partial sucrose conversion is aimed.
- Simple configuration, easy scale-up and simple control of residence time.

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